

#### 22/5/14 M

[This question paper contains 7 printed pages]

Your Roll No. : .....

Sl. No. of Q. Paper : 1812 GC-4

Unique Paper Code : 32341202

Name of the Course : B.Sc.(Hons.)

Computer Science

Name of the Paper : Discrete Structures

Semester : II

Time: 3 Hours Maximum Marks: 75

#### Instructions for Candidates:

- (a) Write your Roll No. on the top immediately on receipt of this question paper.
- (b) **Section A** (Question 1) is compulsory and Carries **35** marks (7×5=35).
- (c) Attempt any four questions from Section

  B (Question 2-7)
- (d) Parts of a question must be answered together.
- (e) Symbols have their usual meanings.

1812

## SECTION - A

(a) Among 100 students, 32 study mathematics, 20 study physics, 45 study biology, 15 study mathematics and biology, 7 study mathematics and physics, 10 study physics and biology and 30 do not study any of the three subjects.

GI

G3

(i) Find the number of students studying all three subjects.

(ii) Find the number of students studying exactly one of the 3 subjects.

(b) Let  $A = \{1,2,3,4,5,6,7\}$  and  $R = \{(x,y) : x-y \text{ is divisible by 3}\}$ . show that R is an equivalence relation.

(d) Define Bipartite Graph and Complete Bipartite Graph. Check whether the graph  $C_6$  is Bipartite or not? Justify your answer.

(e) Determine the numeric function for the following generating function:

5

$$A(Z) = 1/(5-6Z-Z^2)$$

(f) Show that the following system is inconsistent:

$$P \rightarrow Q, P \rightarrow R, Q \rightarrow \neg R, P$$

(g) Use Master method to find the asymptotic bounds for the following recurrence 5  $T(n) = 2T(n/2)+n^{2}$ 

N

w

### SECTION - B

# 2. (a) Show that:

1.2<sup>1</sup>+2.2<sup>2</sup>+3.2<sup>3</sup>+.....+n.2<sup>n</sup>=(n-1)2<sup>n+1</sup>+2 by induction. 5

(b) Determine whether the function f is a bijection from R to R. Find  $f \circ g$  and  $g \circ f$  for the functions f and g where  $f(x)=2x^2+3$  and g(x)=x+1. Is  $f \circ g = g \circ f$ ?

3. (a) In how many ways can four students be selected out of twelve students, if: 5

(i) Two particular students are not included at all?

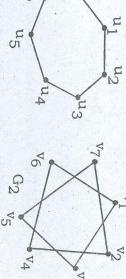
(ii) Two particular students are included

(b) Let A= {1,2,3,4,6,8,9,12,18,24} and let R be a partial ordered relation on A defined by xRy if and only if "x divides y".

(i) Draw the Hasse Diagram of R.

(ii) Find the Maximal and Minimal elements in A.

(a) Define planar graph. Is K<sub>3,3</sub> planar. Justify your Answer. For any connected planar graph; show that v-e+r=2, where v,e and r are the number of vertices, edges and regions of the graph respectively.
(b) What do you mean by graph invariant? Determine whether the graphs G1 and G2 are isomorphic.



**5.** (a) (i) What is the chromatic number of  $C_n$  where  $n \ge 3$  and  $k_{m,n}$ ?

91

(ii)Prove that a connected graph is a tree if and only if the number of vertices in the graph is one more than the number of edges.

(b) Let  $f(n)=n^2+4n$  and  $g(n)=n^2$ ,  $n \ge 0$ . Show that f(n)=O(g(n))

CI

P.T.O

1812

(ii) Show that

raining"

 $\neg (p \leftrightarrow Q) \equiv (P \lor Q) \land \neg (P \land Q)$ 

0 (a) Solve the following recurrence relation:  $a_r-7a_{r-1}+10a_{r-2}=3^r$ , given that  $a_0=0$  and  $a_1=1$ .

(b) Suppose that the number of bacteria in a

colony triples every hour.

(i) Set-up a recurrence relation for the elapsed. number of bacteria after n hours have

(ii) If 100 bacteria are used to begin a new the colony in 10 hours? colony, how many bacteria will be in

7. (a) Show the validity of the following get the job or he will not work hard promotion, then he will be happy. He will hard, then he will be promoted. If Ram gets argument: If Ram gets the job and works not be happy. Therefore, either he will not

9